SOLUTIONS	
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2018
UNIT TEST 3

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paper

MATHEMATICS METHODS Year 11

Section Two: Calculator-assumed

Student name	 	
Teacher name		

Time and marks available for this section

Reading time before commencing work:

3 minutes

Working time for this section:

30 minutes

Marks available:

30 marks

Materials required/recommended for this section To be provided by the supervisor

This Question/Answer Booklet
Formula Sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters

Special items:

drawing instruments, templates, and up to three calculators approved

for use in the WACE examinations

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Instructions to candidates

- 1. Write your answers in this Question/Answer Booklet.
- 2. Answer all questions.
- 3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specific to a particular question.
- 4. Supplementary pages for the use of planning/continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 5. **Show all your working clearly**. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.

(4 marks)

Consider the circle described by the relationship:

$$x^2 + y^2 = 14x - 8y + 16$$

(a) Determine the centre and radius of the circle.

(3 marks)

$$x^{2}-14x+y^{2}+8y=16$$
 $x^{2}-14x+44-49+y^{2}+8y+16-16=16$
 $(x-7)^{2}+(y+4)^{2}-65=16$
 $(x-7)^{2}+(y+4)^{2}=81$ (completing the square for x and y)

Lentre is $(7,-4)$ (for culculating centre)

radius is $\sqrt{8}=9$ (for calculating radius)

(b) Determine the domain for the relationship.

(1 mark)

$$1-9 \le x \le 7+9$$
domain is $\{x \in \mathbb{R}: -2 \le x \le 16\}$

$$\sqrt{\text{furcalculuting domain}}$$

$$-2 < x \le 16$$

$$\sqrt{167} \times 7 -2 \text{ also OK.}$$

(4 marks)

Determine the equation of the image of the graph of $v = \sqrt{x}$ when the following sequence of transformations has been applied: a reflection in the v axis, followed by a translation of 3 units right. (2 marks)

refletion in yatir y=5-x

V (for correct reflection in yatis)

Franslution 3 units

right $y=\sqrt{-(x-3)}$ or $y=\sqrt{-x+3}$

(for lonect final answer)

Determine the equation of the image of the graph of:

$$y = 3x^3 + x^2 - 5x + 2$$

when the graph has firstly been reflected in the x axis and then translated 2 units up. (2 marks)

(reflected

from slated

$$y = -(3x^{3} + x^{2} - 5x + 2) + 2$$
 (by correct
 $y = -3x^{3} - x^{2} + 5x$ final answer)

(2 marks)

A polynomial P(x) has been factorised as follows:

$$P(x) = (x-1)^2(3x+4)$$

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For the standard form of P(x), that is with the brackets expanded, determine the following:

(a) The coefficient of the x term.

(1 mark)

expand using Classpad P(x)= 32-2x-5x+4

Coefficient of x term is -5

(Krgiving correct wefficient)

(b) The constant term.

(1 mark)

Longhart term is 4

V (for giving correct constant learn)

(4 marks)

The angles A and B are both obtuse angles (that is, they are both in the range $90^{\circ} < \theta < 180^{\circ}$), such that:

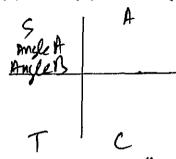
6

$$\sin(A) = \frac{3}{5} \quad \text{and} \quad \cos(B) = \frac{-12}{13}$$

Determine the exact values of the following:

(a) cos(A) and sin(B).

(2 marks)



angles A and B are in second quadrant so sine is positive and his is negative

5/A F 3 4/4

13 5 n

605A=-4 5

Sin B= 5

W(hr los A)

~ (Ar sin B)

(b) sin(A-B).

(2 marks)

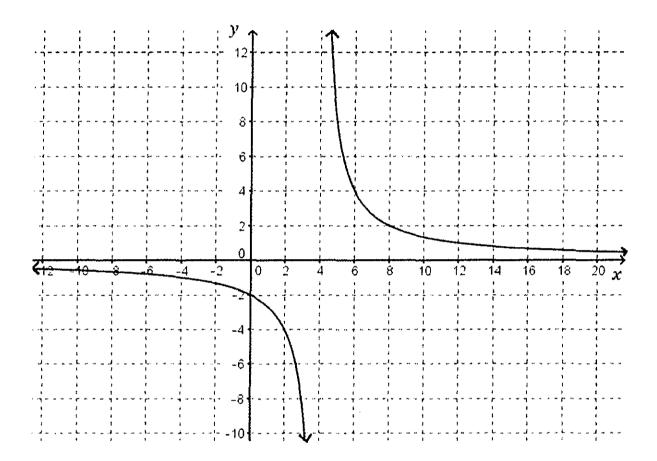
Sin (A-B) = Sin A cosB - los A sin B = $\frac{3}{5} \times \left(\frac{-12}{13}\right) - \left(\frac{-4}{5}\right) \times \left(\frac{5}{13}\right)$ ~ (correct expansion) = $\frac{-36}{65} + \frac{20}{65}$ = $\frac{-16}{65}$ ~ (final answer)

(3 marks)

The equation of the curve in the graph below is in the form:

$$y = \frac{a}{x - b}$$

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Determine the values of a and b.

Verkal asymptote at x=4 so b=4 (correct value 4b) $y=\frac{9}{2-4}$ use part(0,-2) $-2=\frac{9}{0-4}$ so a=8 (correct value 4a)

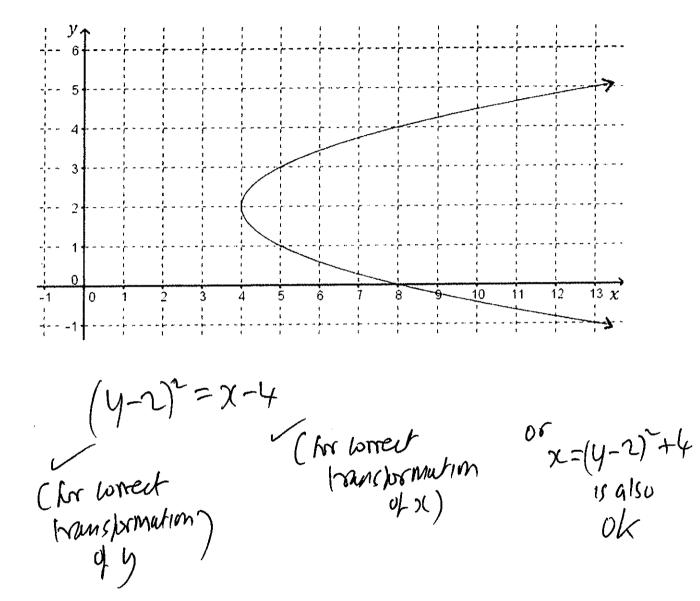
(b) If the curve is subject to a dilation of scale factor 4 parallel to the y axis, give the equation of the horizontal asymptote of the new curve. (1 mark)

y=0 (hr wheet answer)

(2 marks)

The following graph shows $y^2 = x$ after it has been translated either up, down, left or right, or a combination of these. Give the equation of the curve shown in the graph.

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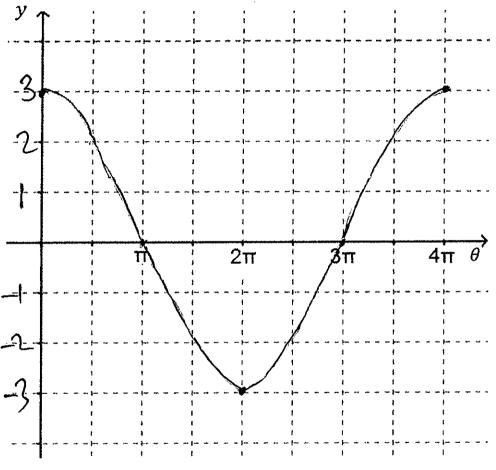


(2 marks)

Use the axes below to sketch the following graph for $0 \le \theta \le 4\pi$:

$$y = 3\cos\left(\frac{\theta}{2}\right)$$

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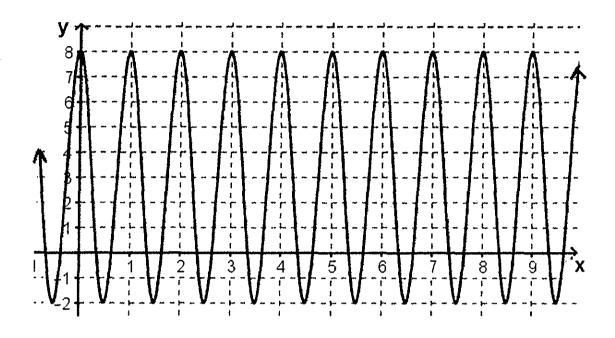


V (correct x axis
intercepts)

(correct max and
min values)

(3 marks)

Determine the equation of the following cosine function:



fransluled 3 units up

amplitude=5

(6 marks)

The depth in water, in metres, in a harbour at a certain point at time t hours is given by D(t), where:

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$$D(t) = 8 + 2\sin\left(\frac{\pi t}{6}\right), \quad 0 \le t \le 24$$

(a) Determine the period of the function D(t).

(2 marks)

period of sine function = 35, b=17/6

period = 24/16

= 2/16

= 12 hours (gives final answer period)

by period)

(b) Give the value of t when the depth of the water is first 9 metres.

(2 marks)

9=8+25cn(15) (setup hasic equation)
Solve on
Clustered t=1 hour (Sive how answer)

(c) For how many hours in the 24 hour period under consideration, is the depth at least 9 metres? (2 marks)

(for showing appropriate working out)

time of depth at least 9 metres = 4+4 = 8 hours (for final answer)

Additional	working	space
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Question	number:	

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CALCULATOR-ASSUMED

Additional working space

Question number:_____